

Clear All;

"Za prvu oblast vazi: $\Delta\varphi_1 = -\frac{\rho}{\epsilon_0}$ odnosno $\frac{1}{r} \frac{d}{dr} (r \frac{d\varphi}{dr}) = -\frac{\rho}{\epsilon_0}$ ";

"Za drugu oblast vazi: $\Delta\varphi_2 = 0$ odnosno $\frac{1}{r} \frac{d}{dr} (r \frac{d\varphi}{dr}) = 0$ ";

"Rjesavanjem dobijamo:";

$\varphi_1 = -\frac{\rho}{4 * \epsilon_0} * r^2 + C1 * \ln(r) + C2 = \varphi_0$ (na osnovu gr. uslovaza prvu oblast);

$\varphi_2 = C3 * \ln(r) + C4$ (na osnovu gr. uslova za drugu oblast);

"Takodje vazi: $D1n = D2n$ odnosno $\epsilon_1 E1 = \epsilon_2 E2$ tj. $\epsilon_1 (-\text{grad}\varphi_1) = \epsilon_2 (-\text{grad}\varphi_2)$ ";

"Na granici dvije oblasti vazi $\varphi_1(b) = \varphi_2(b)$.";

"Na osnovu ovih jednačina dobijamo:";

Rez = Flatten[Solve[{ $\varphi_0 = -\frac{\rho}{4 * \epsilon_1} * a^2 + C1 * \text{Log}[a] + C2$, $0 = C3 * \text{Log}[c] + C4$,
 $-\frac{\rho}{4 * \epsilon_1} * b^2 + C1 * \text{Log}[b] + C2 = C3 * \text{Log}[b] + C4$, $(-\frac{\rho}{2} * b + \epsilon_1 * \frac{C1}{b}) = \epsilon_2 * \frac{C3}{b}$ },
{C1, C2, C3, C4}]]];

Print["C1= ", FullSimplify[Together[C1 /. Rez]]]

Print["C2= ", FullSimplify[Together[C2 /. Rez]]]

Print["C3= ", FullSimplify[Together[C3 /. Rez]]]

Print["C4= ", FullSimplify[Together[C4 /. Rez]]]

$$C1 = \frac{\epsilon_2 ((a-b)(a+b)\rho + 4\epsilon_1\varphi_0) + 2b^2\epsilon_1\rho(\text{Log}[b] - \text{Log}[c])}{4\epsilon_1(\epsilon_2\text{Log}[a] + (\epsilon_1 - \epsilon_2)\text{Log}[b] - \epsilon_1\text{Log}[c])}$$

$$C2 = \frac{(a^2\rho + 4\epsilon_1\varphi_0)((\epsilon_1 - \epsilon_2)\text{Log}[b] - \epsilon_1\text{Log}[c]) + b^2\rho\text{Log}[a](\epsilon_2 - 2\epsilon_1\text{Log}[b] + 2\epsilon_1\text{Log}[c])}{4\epsilon_1(\epsilon_2\text{Log}[a] + (\epsilon_1 - \epsilon_2)\text{Log}[b] - \epsilon_1\text{Log}[c])}$$

$$C3 = \frac{(a-b)(a+b)\rho + 4\epsilon_1\varphi_0 + 2b^2\rho(-\text{Log}[a] + \text{Log}[b])}{4(\epsilon_2\text{Log}[a] + (\epsilon_1 - \epsilon_2)\text{Log}[b] - \epsilon_1\text{Log}[c])}$$

$$C4 = -\frac{((a-b)(a+b)\rho + 4\epsilon_1\varphi_0 + 2b^2\rho(-\text{Log}[a] + \text{Log}[b]))\text{Log}[c]}{4(\epsilon_2\text{Log}[a] + (\epsilon_1 - \epsilon_2)\text{Log}[b] - \epsilon_1\text{Log}[c])}$$